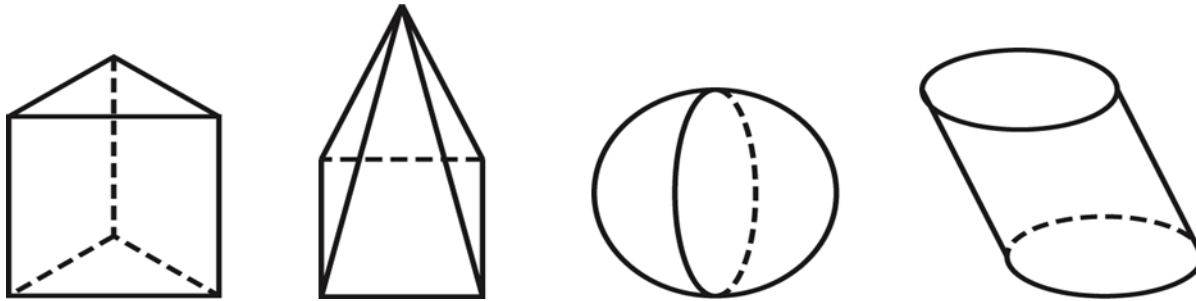


# Section 11-4 Geometry in Three Dimensions

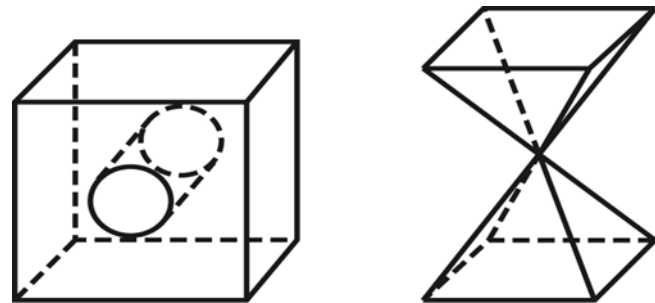
- Simple closed surfaces and polyhedra.
- How to draw three-dimensional shapes.
- Why there are only five regular polyhedra.
- Simple closed surfaces that are not polyhedra.

# Simple Closed Surfaces (1 of 2)

A **simple closed surface** has exactly one interior, no holes, and is hollow.



These two figures are not simple, closed surfaces.



# Simple Closed Surfaces (2 of 2)

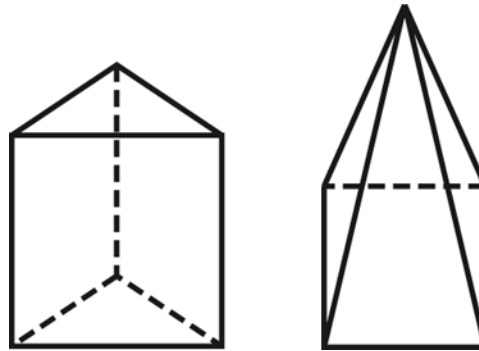
**Sphere** – the set of all points at a given distance from a given point (the **center**)

**Solid** – the set of all points on a simple closed surface together with all interior points

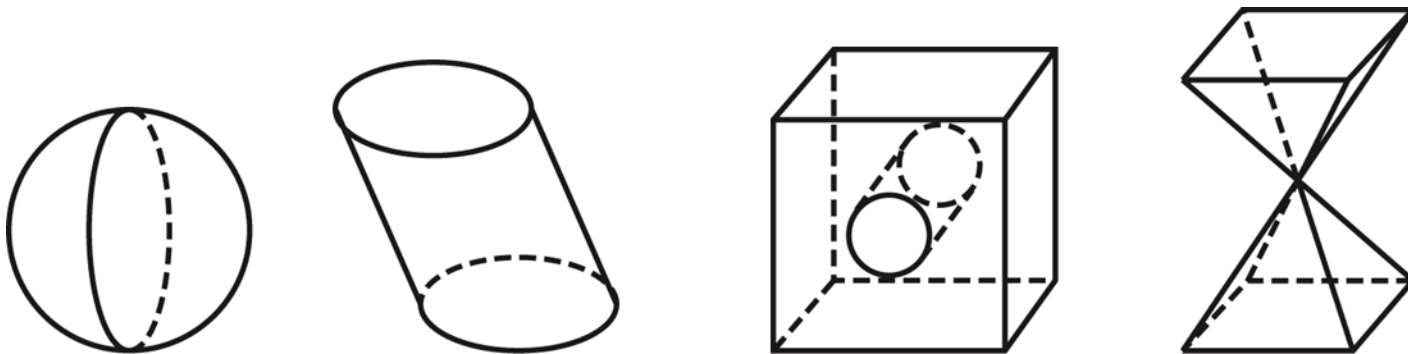
**Polyhedron** – a simple, closed surface made up of polygonal regions (**faces**). The vertices of the polygonal regions are the **vertices** of the polyhedron. The sides of the polygonal regions are called the **edges** of the polyhedron.

# Polyhedra

Polyhedra:



Not polyhedra:

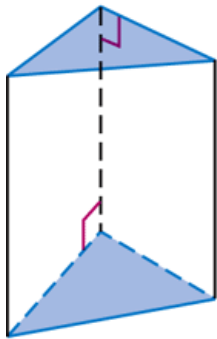




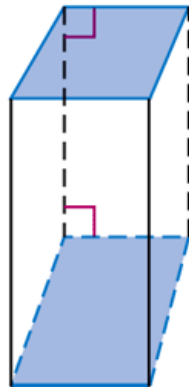
# Prisms (2 of 2)

**Right prism** – lateral faces are perpendicular to the bases. (lateral faces are rectangles)

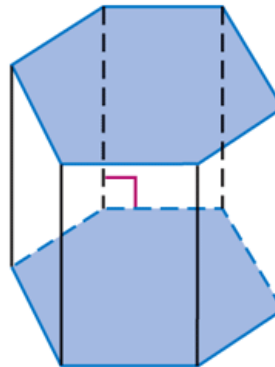
**Oblique prism** – lateral faces are not perpendicular to the bases. (lateral faces are parallelograms)



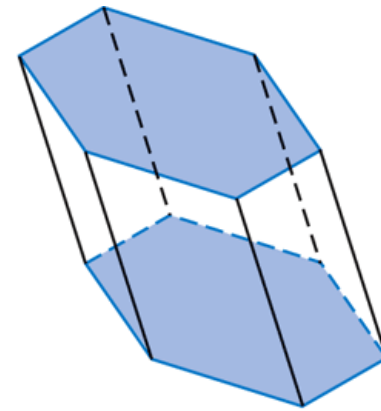
Triangular  
right prism



Quadrilateral  
right prism



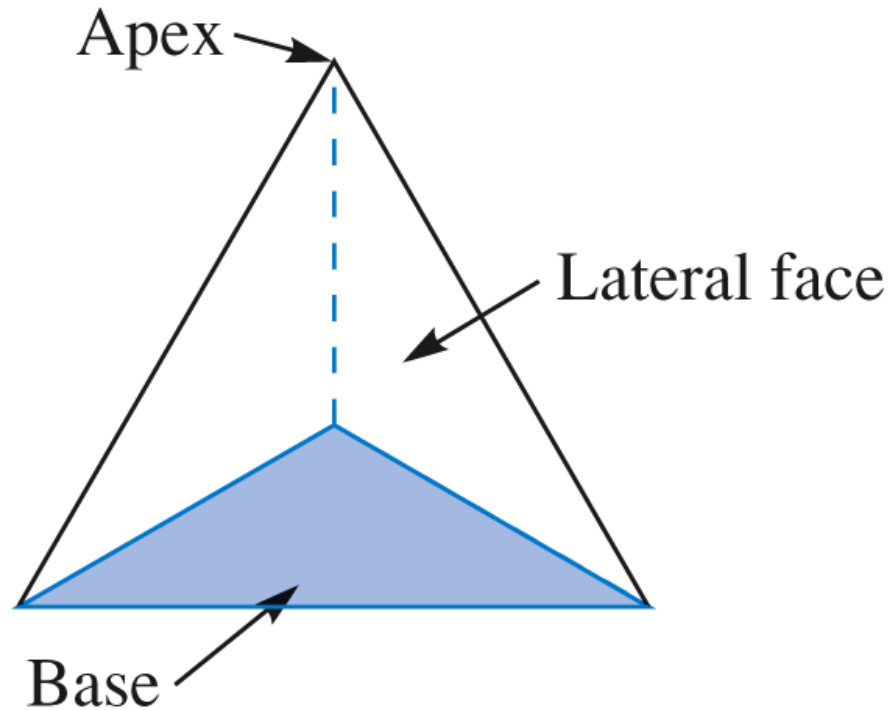
Hexagonal  
right prism



Hexagonal  
oblique prism

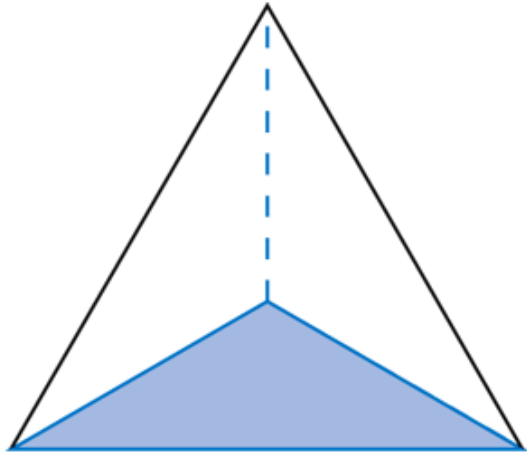
# Pyramids (1 of 2)

A **pyramid** is a polyhedron determined by a polygon and a point not in the plane of the polygon.

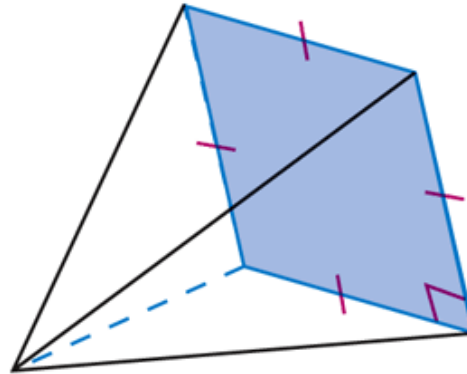


# Pyramids (2 of 2)

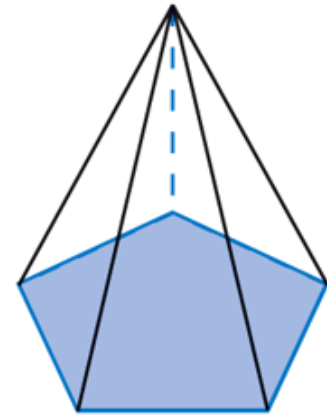
**Right pyramid** – lateral faces are congruent isosceles triangles.



Triangular pyramid



Square pyramid

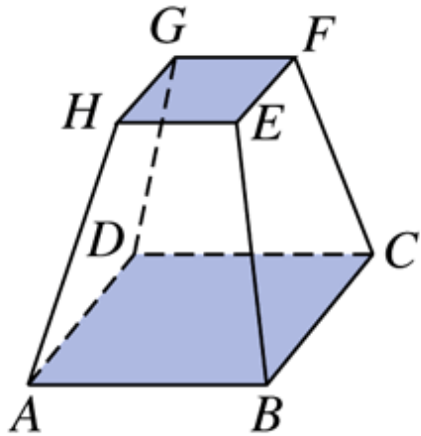


Pentagonal pyramid

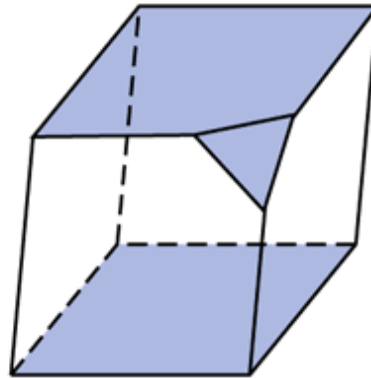


# Truncated Polyhedron

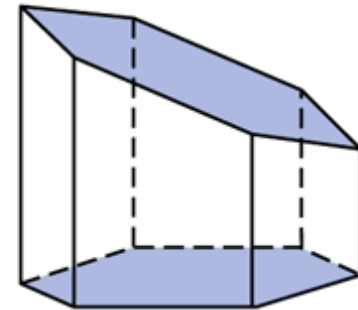
If one or more corners of a polyhedron is removed by an intersecting plane or planes, the polyhedron is a **truncated polyhedron**.



Truncated square  
pyramid with  
parallel bases



Truncated cube



Truncated prism

# Regular Polyhedra (1 of 5)

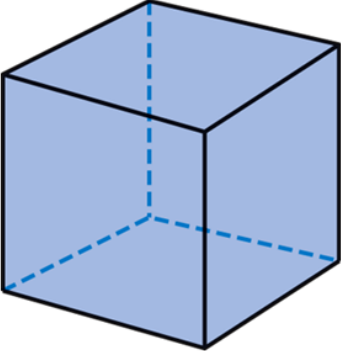
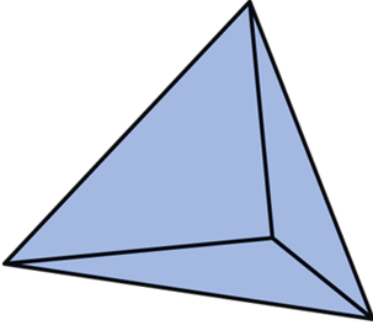
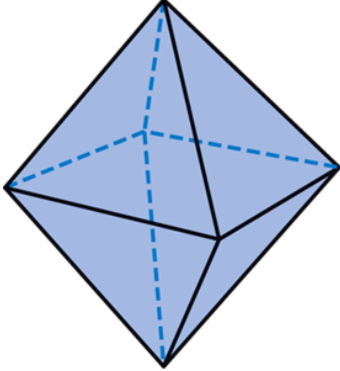
**Convex polyhedron** – a polyhedron in which a segment connecting any two points in the interior of the polyhedron is completely contained within the interior of the polyhedron.

**Concave polyhedron** - a polyhedron that is not convex

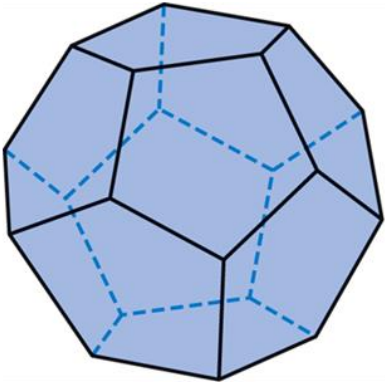
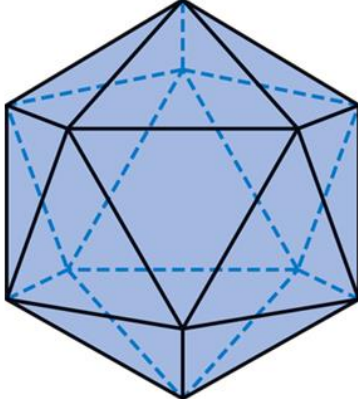
**Regular polyhedron** – a convex polyhedron whose faces are congruent regular polygonal regions such that the number of edges that meet at each vertex is the same for all the vertices of the polyhedron.

# Regular Polyhedra (Platonic Solids)




(2 of 5)

<b>Cube</b>	<b>Tetrahedron</b>	<b>Octahedron</b>
		



# Regular Polyhedra (3 of 5)

<b>Dodecahedron</b>	<b>Icosahedron</b>
	

# Regular Polyhedra (4 of 5)

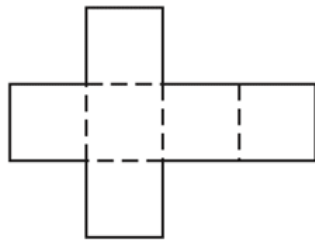
Polygon	Measure of an Interior Angle	Number of Polygons at a Vertex	Sum of the Angles at the Vertex	Polyhedron Formed	Model
Triangle	60°	3	180°	<b>Tetrahedron</b>	
Triangle	60°	4	240°	<b>Octahedron</b>	
Triangle	60°	5	300°	<b>Icosahedron</b>	

# Regular Polyhedra (5 of 5)

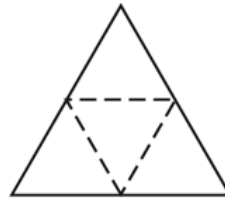
Polygon	Measure of an Interior Angle	Number of Polygons at a Vertex	Sum of the Angles at the Vertex	Polyhedron Formed	Model
Square	$90^\circ$	3	$270^\circ$	Cube	
Pentagon	$108^\circ$	3	$324^\circ$	Dodecahedron	

# Nets

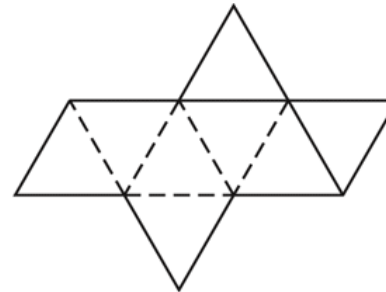
These patterns can be used to construct the five regular polyhedra.



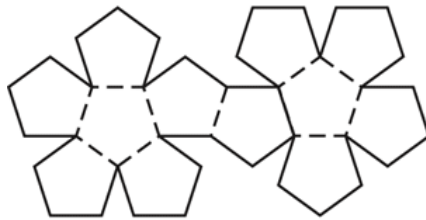
Cube



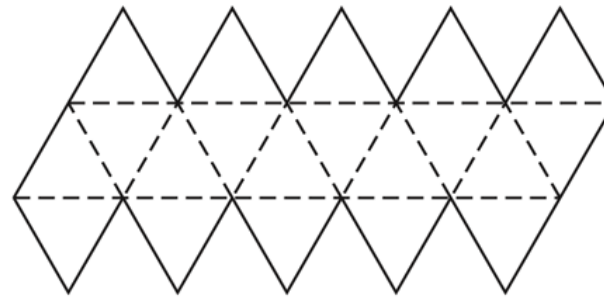
Tetrahedron



Octahedron



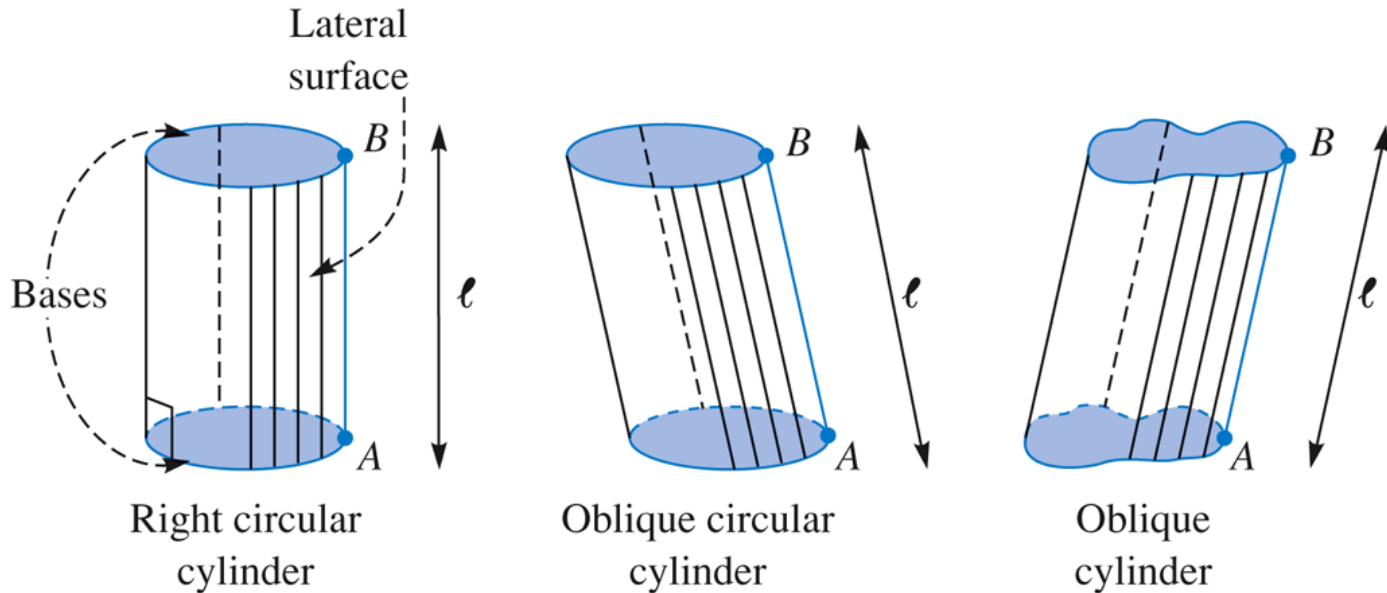
Dodecahedron



Icosahedron

# Cylinders and Cones (1 of 2)

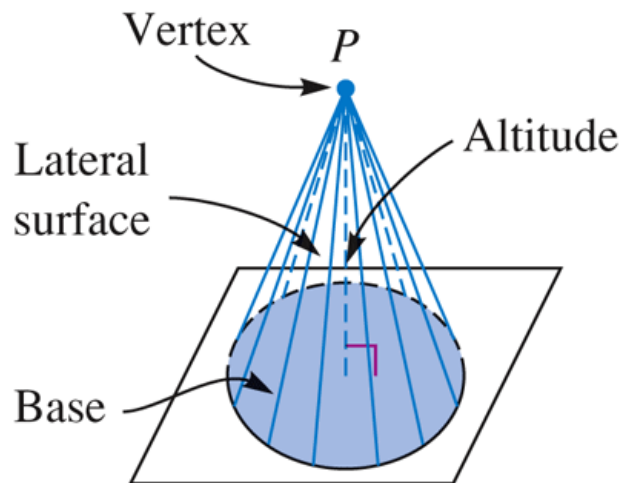
**Cylinder** – a simple, closed surface that is not a polyhedron; formed as a segment  $AB$  parallel to a given line  $l$  traces a planar curve other than a polygon.



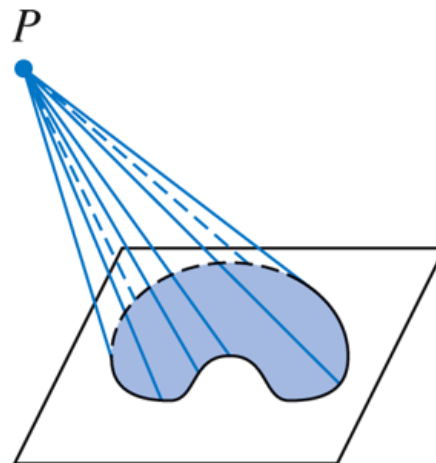


# Cylinders and Cones (2 of 2)

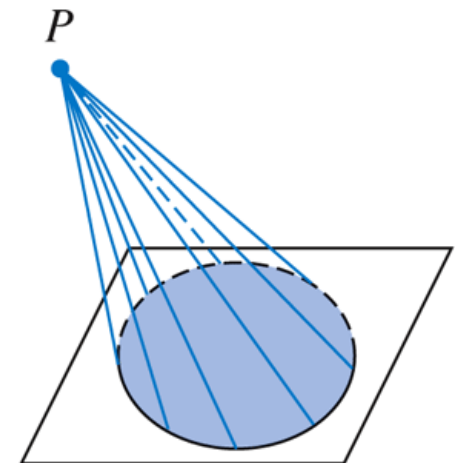
**Cone** – the union of the line segments connecting a point  $P$  with each point of a simple, closed curve, the simple, closed curve, and the interior of the curve.



Right  
circular cone

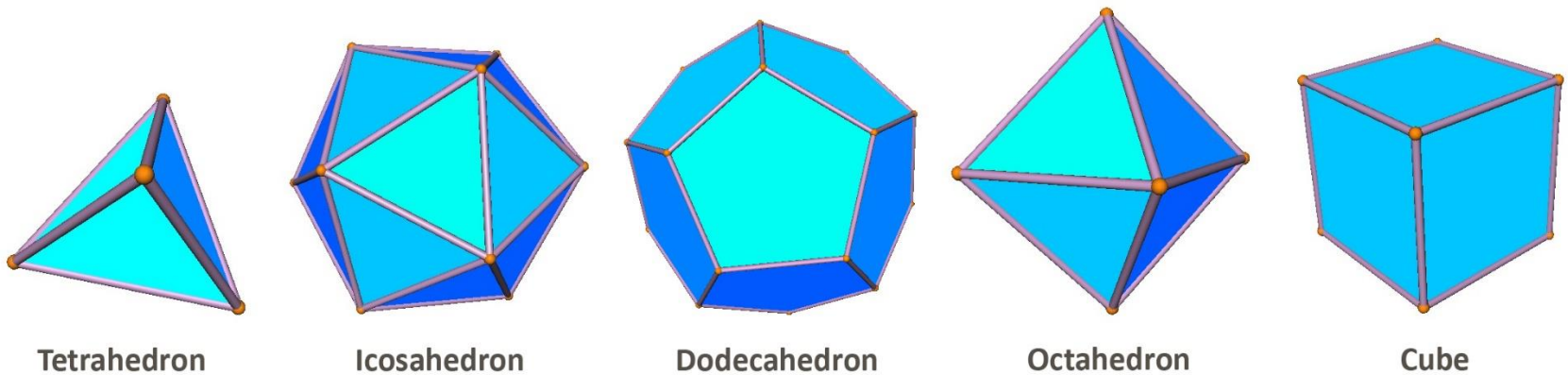


Oblique  
cone



Oblique  
circular cone

# This ends Section 11.4



[This Photo](#) by Unknown Author is licensed under [CC BY-SA-NC](#)